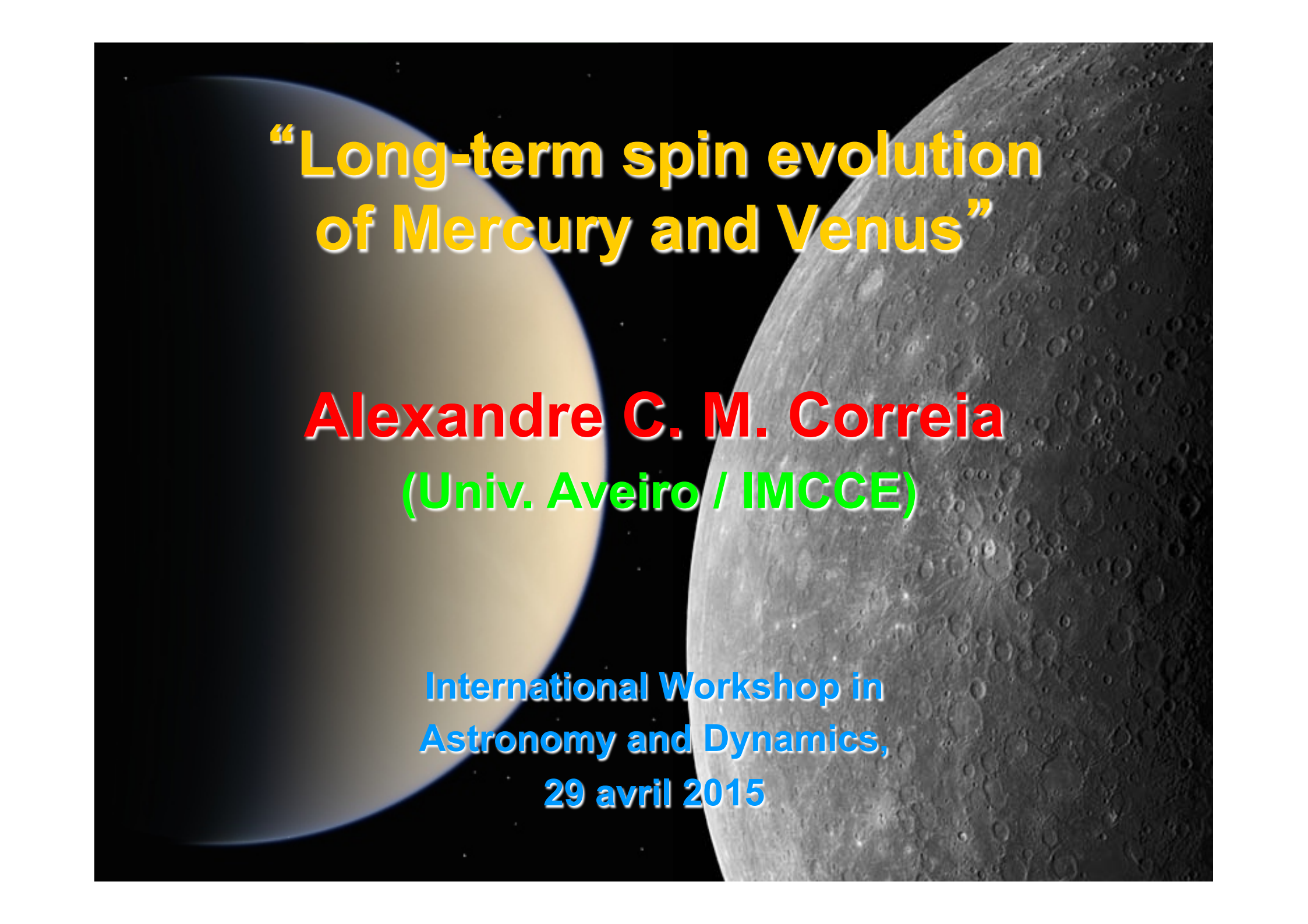




“Long-term spin evolution of Mercury and Venus”

Alexandre C. M. Correia
(Univ. Aveiro / IMCCE)

**International Workshop in
Astronomy and Dynamics,
29 avril 2015**



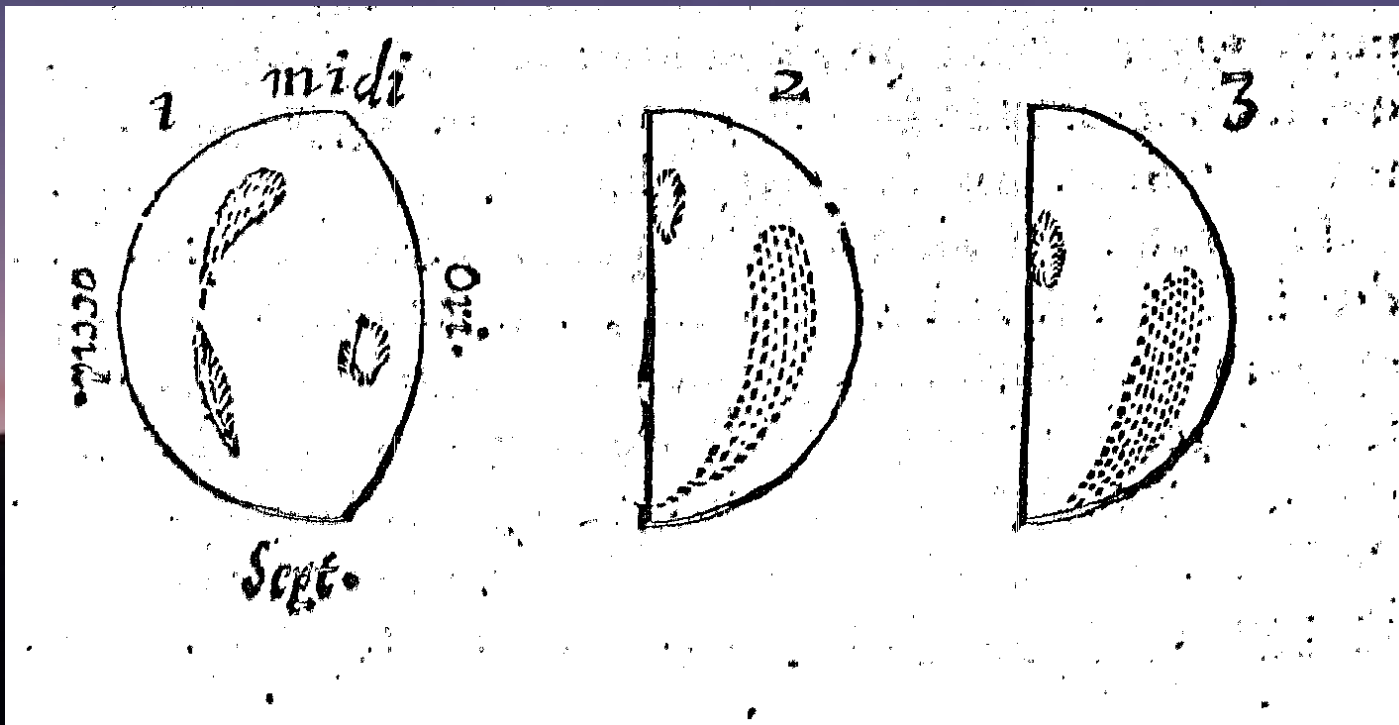
What are the spins of Mercury and Venus?

Venus:

- Jean-Dominique Cassini (1625-1712)

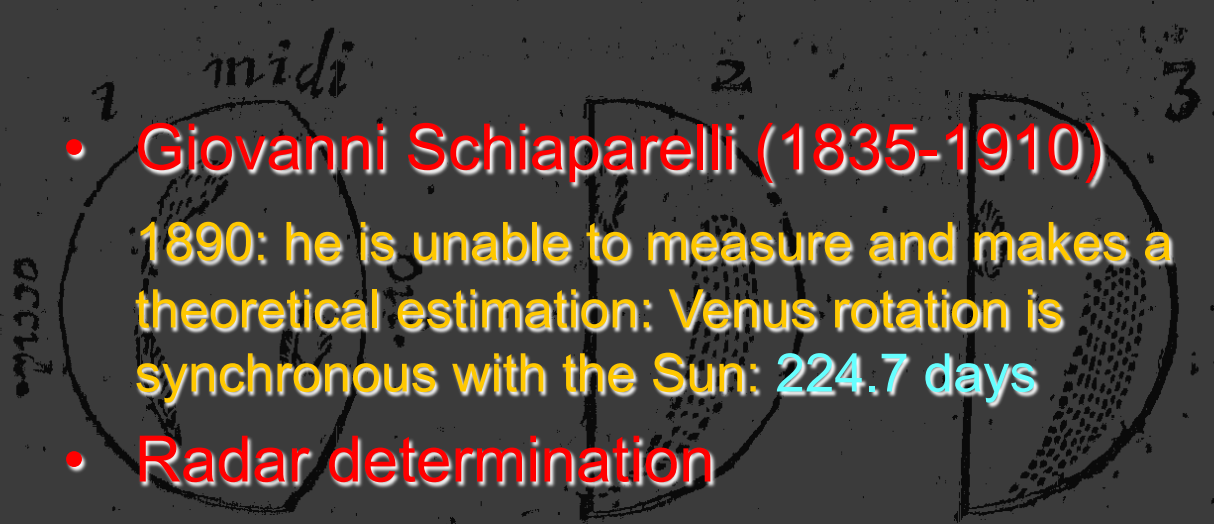
1667: less than 24^h (~ 23^h45^m)

"Mais jusqu'au 28 jour d'Avril [Jacques' birthday], je ne pus remarquer aucune partie luisante semblable à celle que j'avais déjà vue, mais ce jour là, un quart d'heure avant le lever du Soleil, je commençais à revoir sur le disque de cette Planète, dont la moitié ou environ paraissait pour lors éclairée, une partie luisante située auprès de la section"



Venus:

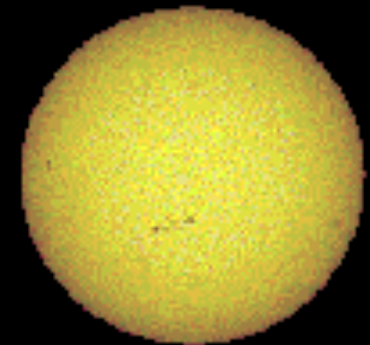
- Jean-Dominique Cassini (1625-1712)
1667: less than 24^h ($\sim 23^h45^m$)
- Francesco de Vico (1805-1848)
1841: $23^h21^m21,934^s$!!!

- 
- Giovanni Schiaparelli (1835-1910)
1890: he is unable to measure and makes a theoretical estimation: Venus rotation is synchronous with the Sun: 224.7 days
 - Radar determination
1962: — 243.02 days !!!

present data

Planet	Period	Obliquity
Mercury	58 day	0,1°
Venus	-243 day	2,7°
Earth	23,93 hour	23,5°
Mars	24,62 hour	25,2°
Jupiter	9,92 hour	3,1°
Saturn	10,66 hour	26,7°
Uranus	-17,24 hour	82,1°
Neptun	16,11 hour	29,6°

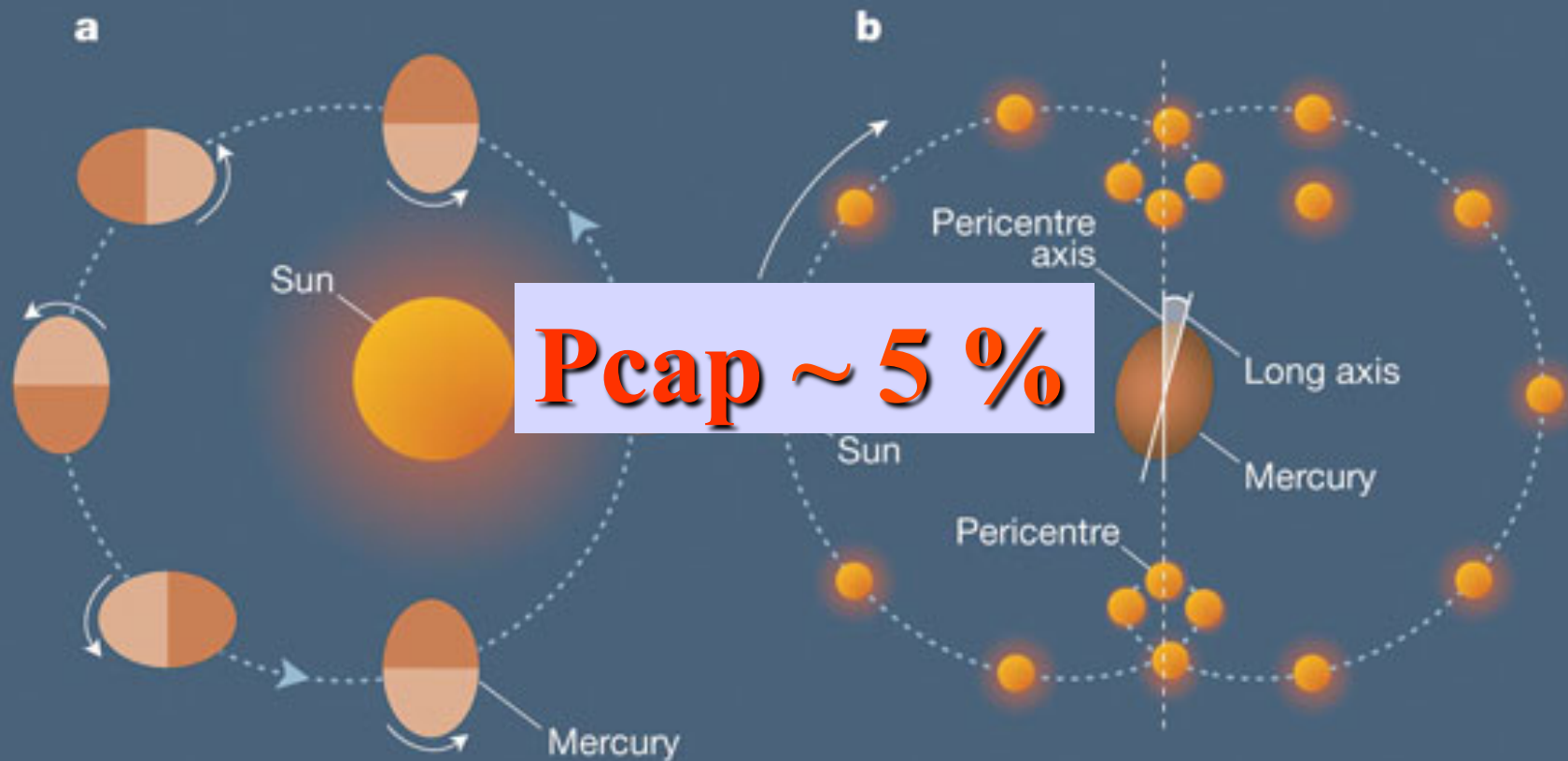
Tidal effect



$P_{\text{orb}} = P_{\text{rot}}$
perpendicular axis
circular orbits

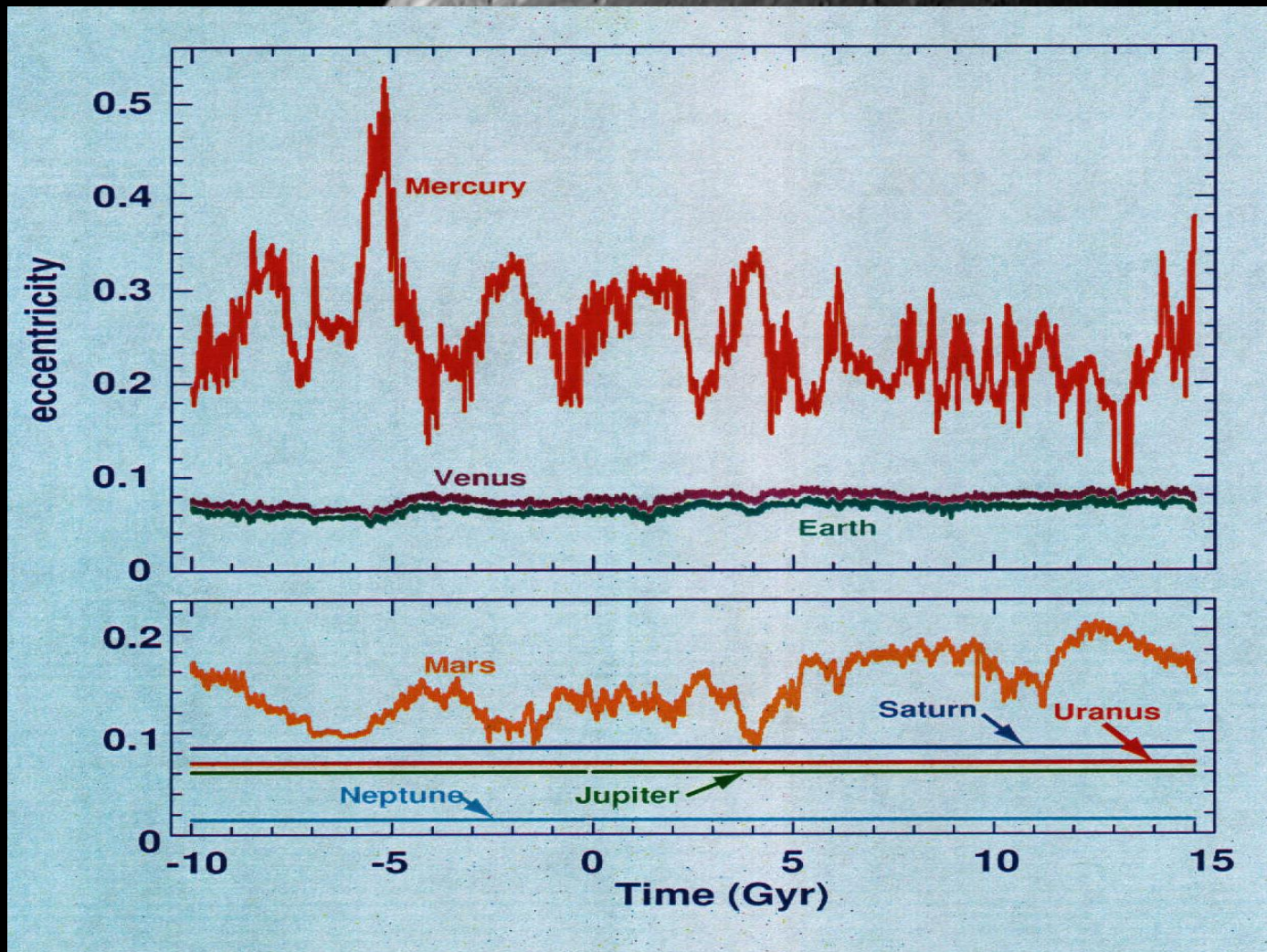
Case of the Moon and
remaining satellites of
the Solar System

Mercury: 3/2 spin-orbit resonance

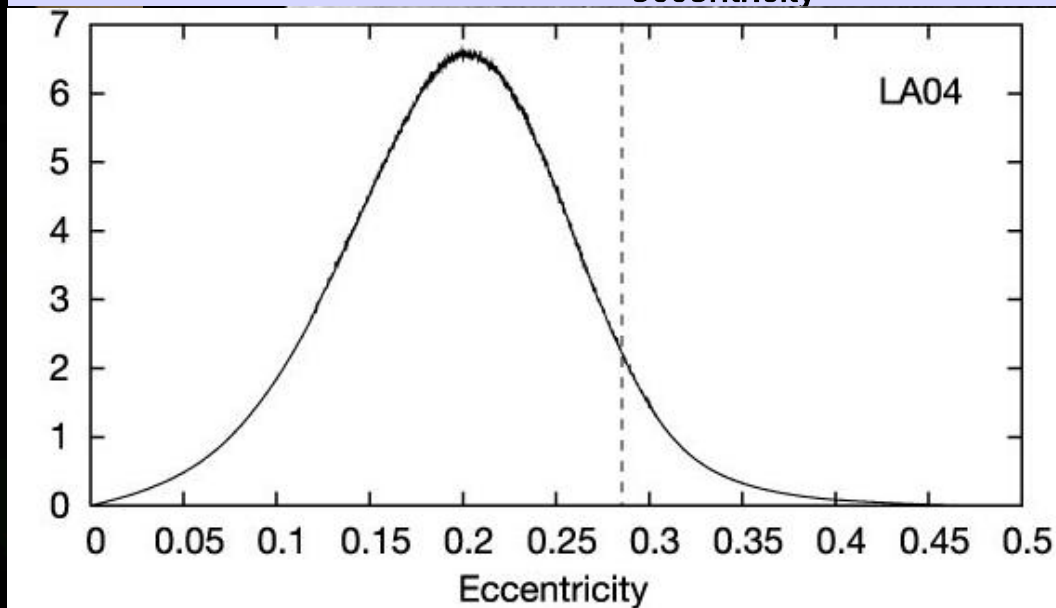
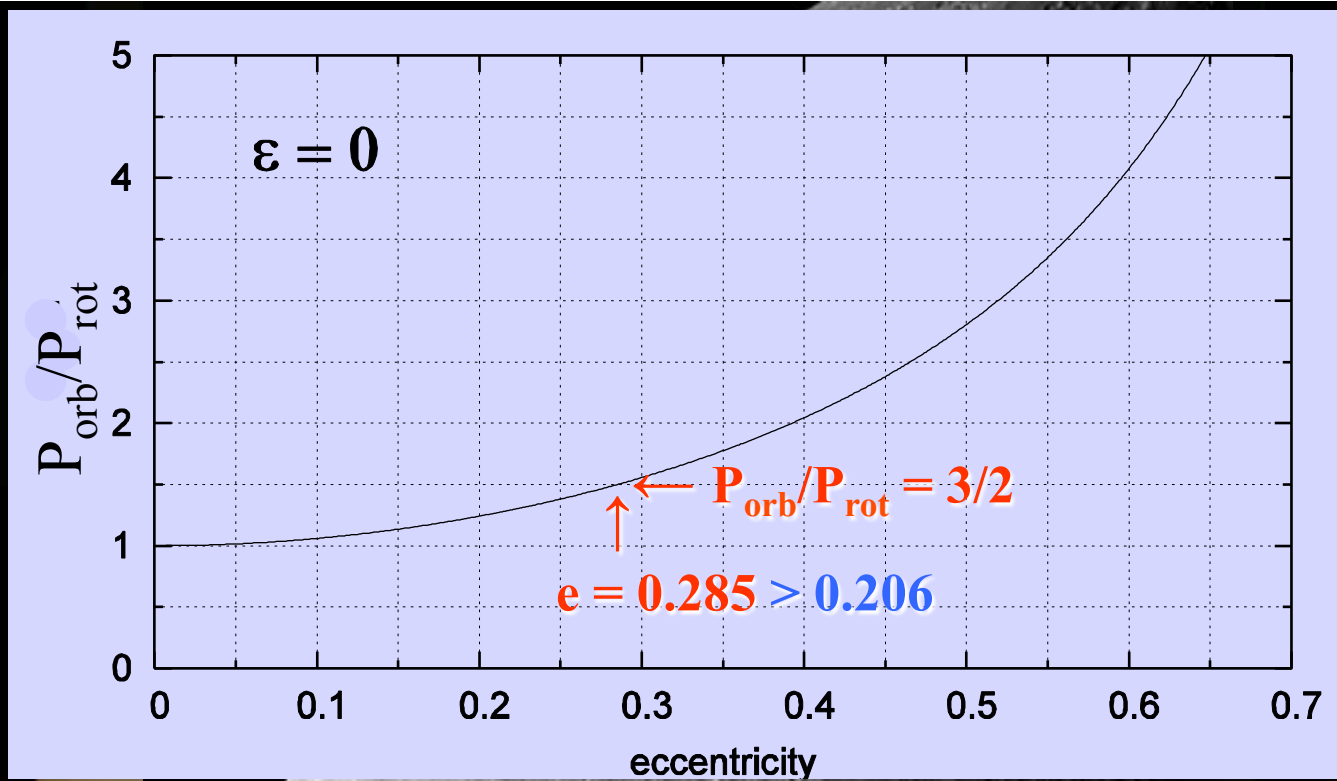


Colombo, 1965,
Goldreich & Peale, 1966

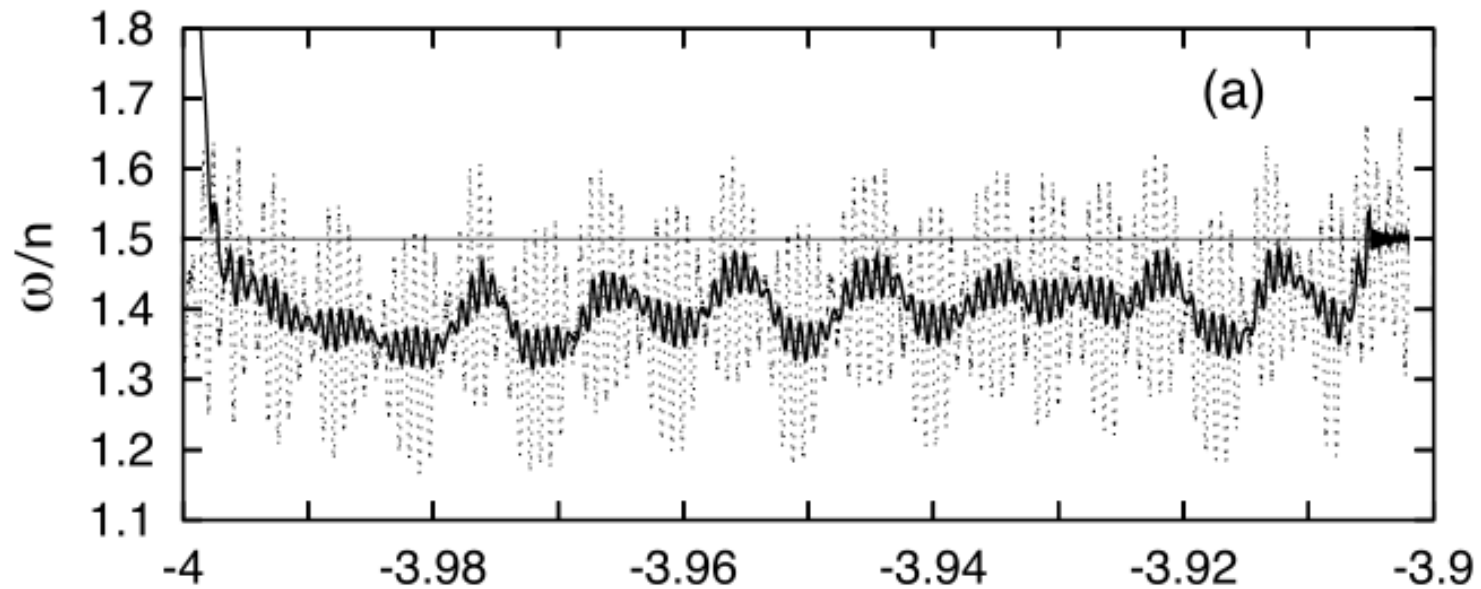
planetary perturbations



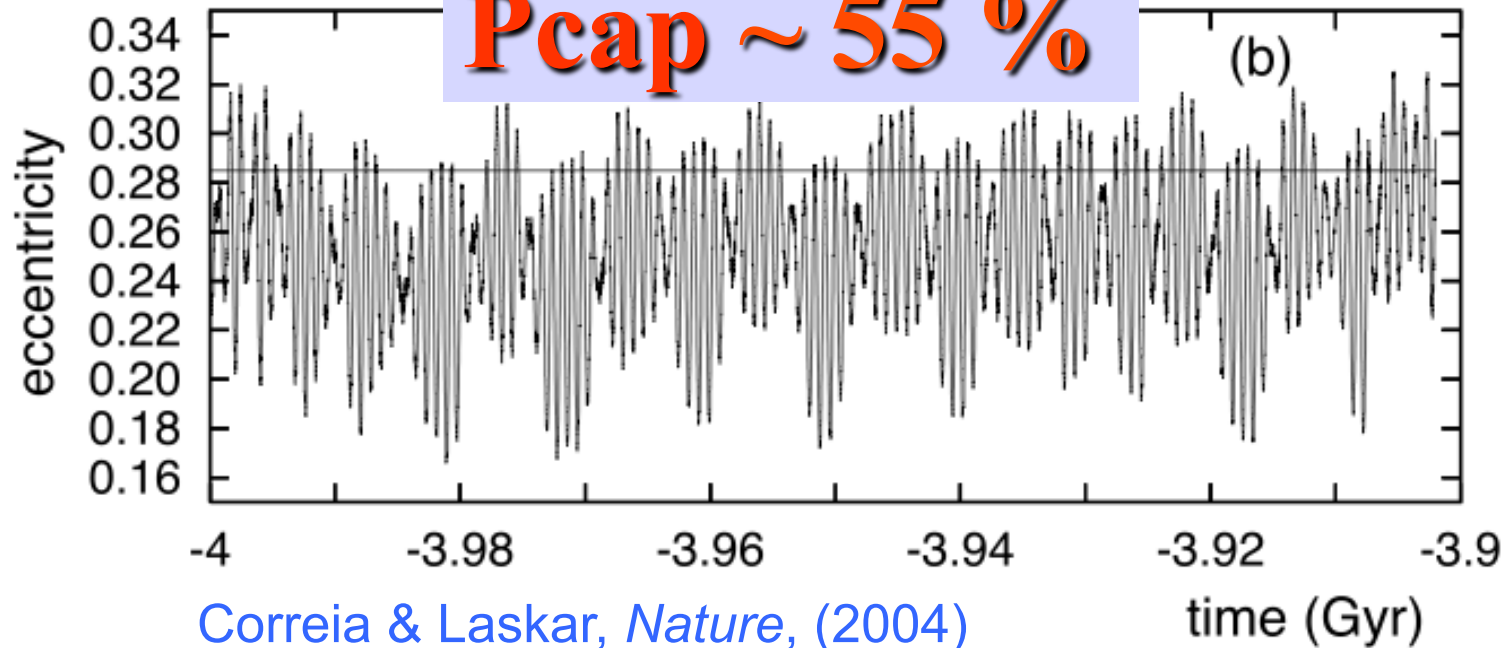
Laskar, 1994



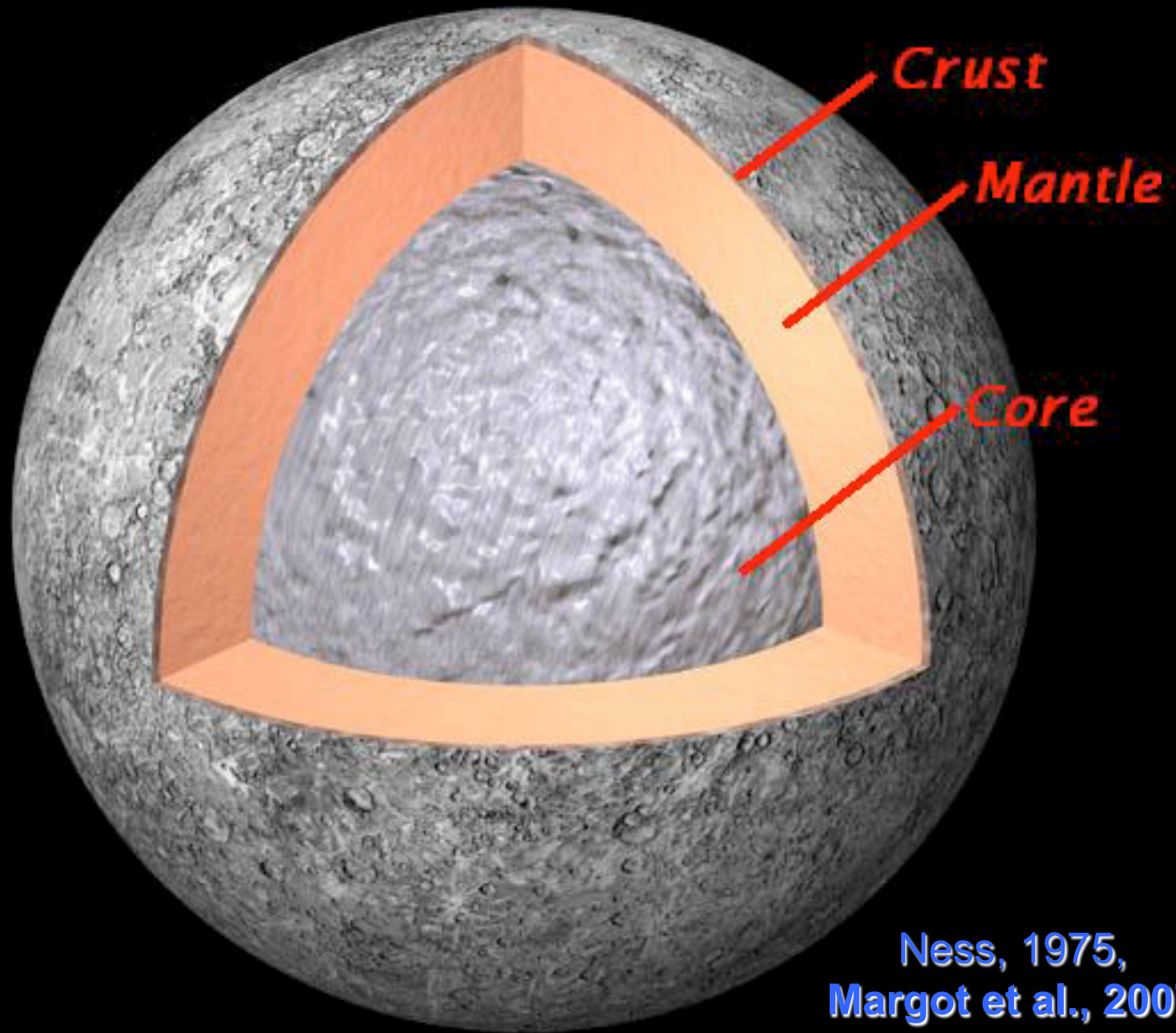
Correia & Laskar,
Nature, 2004



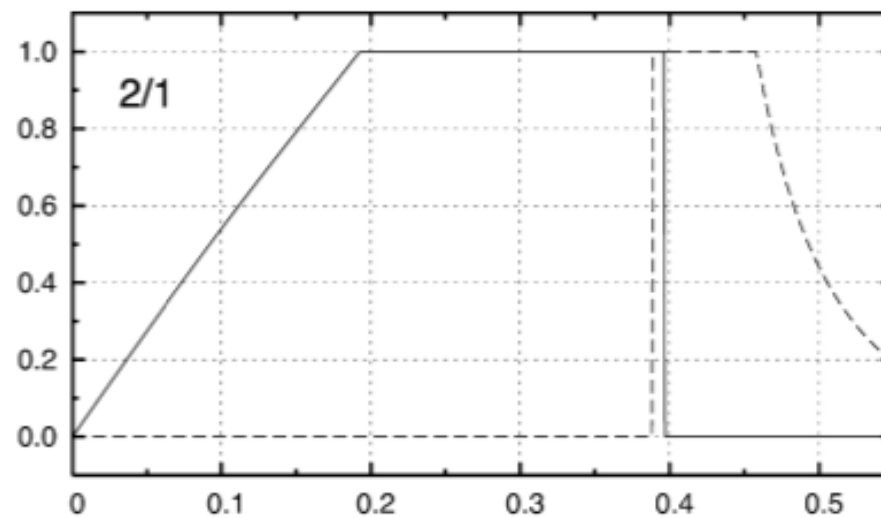
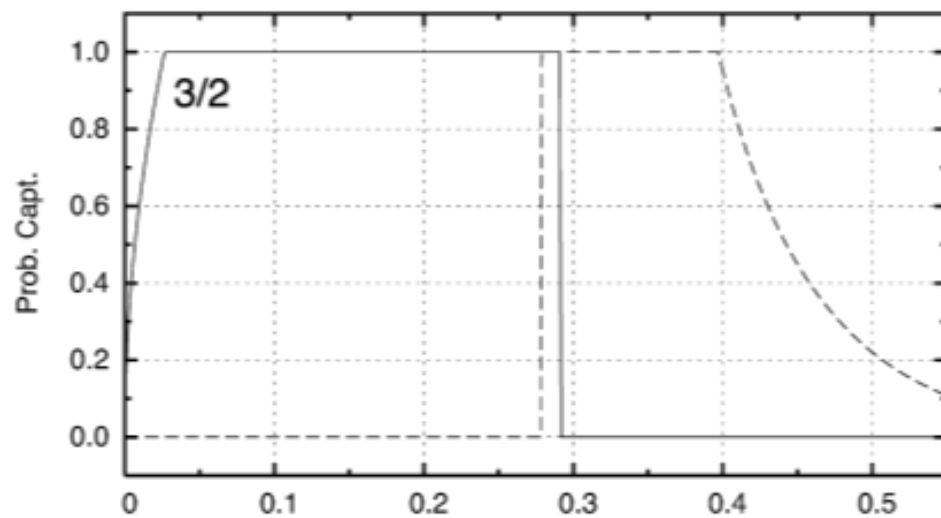
Pcap ~ 55 %



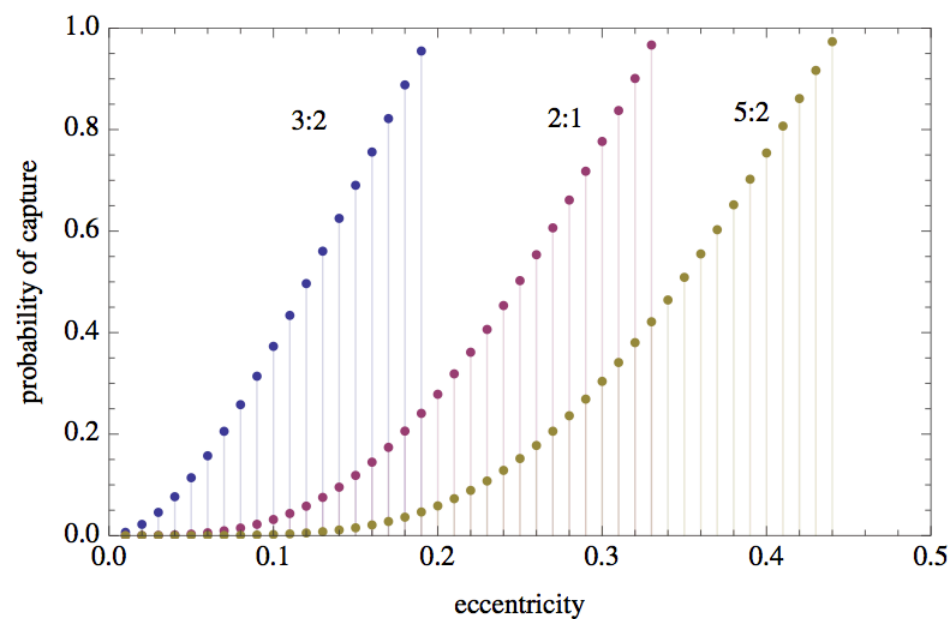
Correia & Laskar, *Nature*, (2004)



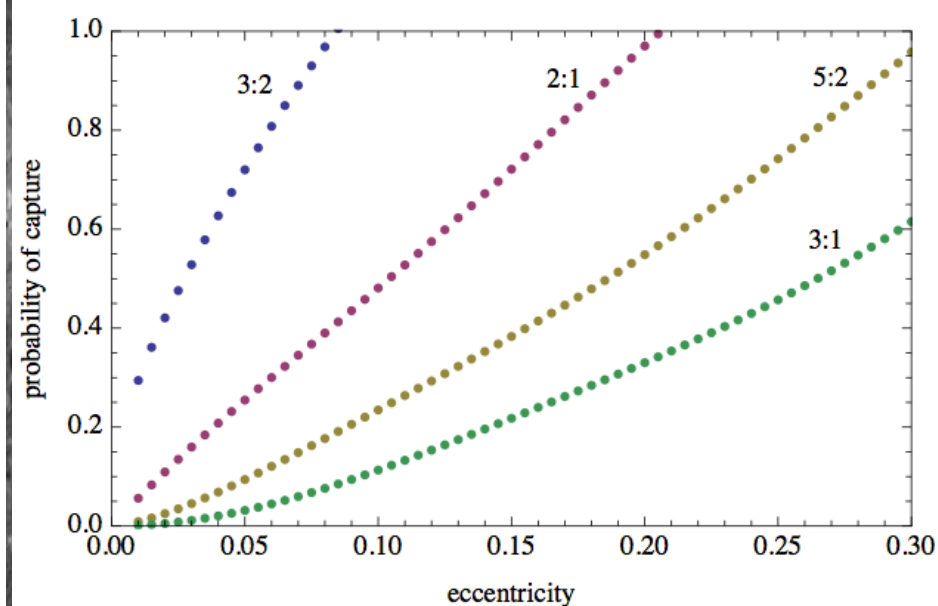
Ness, 1975,
Margot et al., 2007



Correia & Laskar, 2009



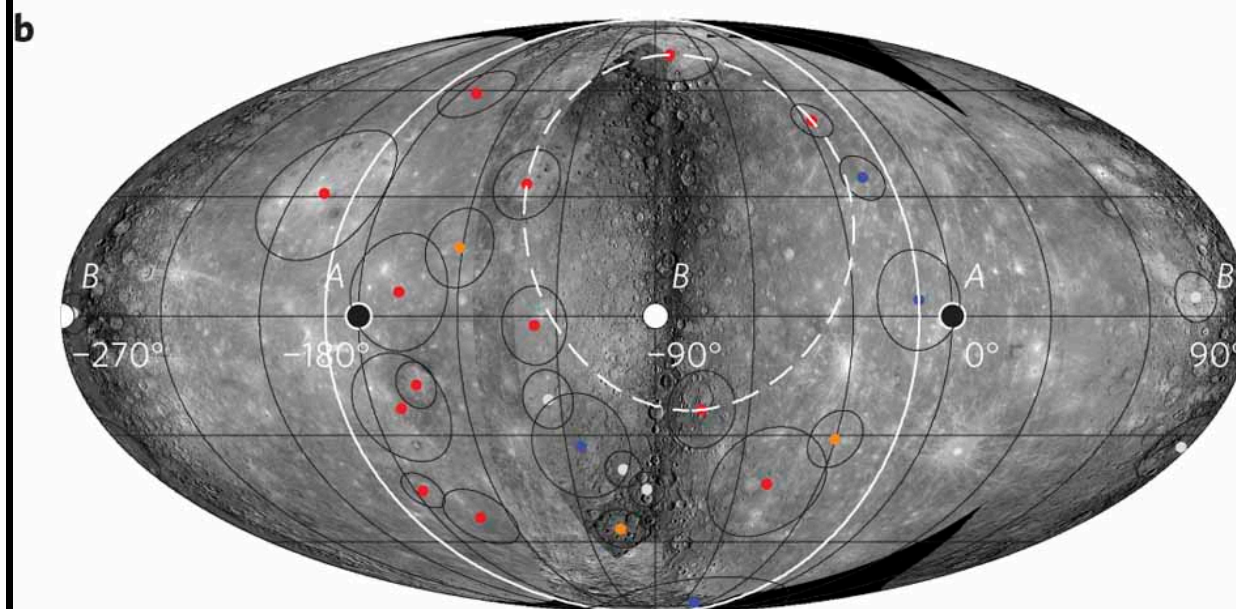
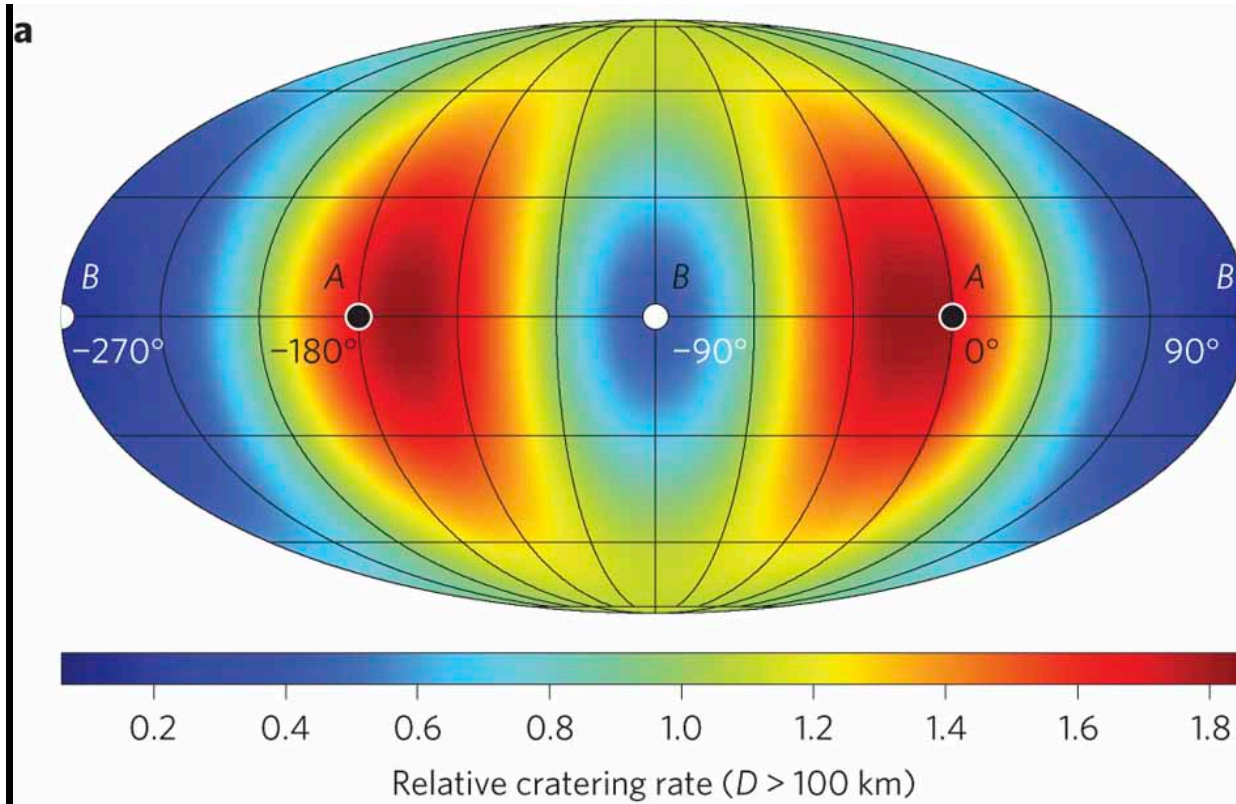
Makarov, 2012



Noyelles et al., 2014

Was Mercury synchro- nous?

Wieczorek, Correia,
Laskar, Rambaux,
Nature Geo, 2012



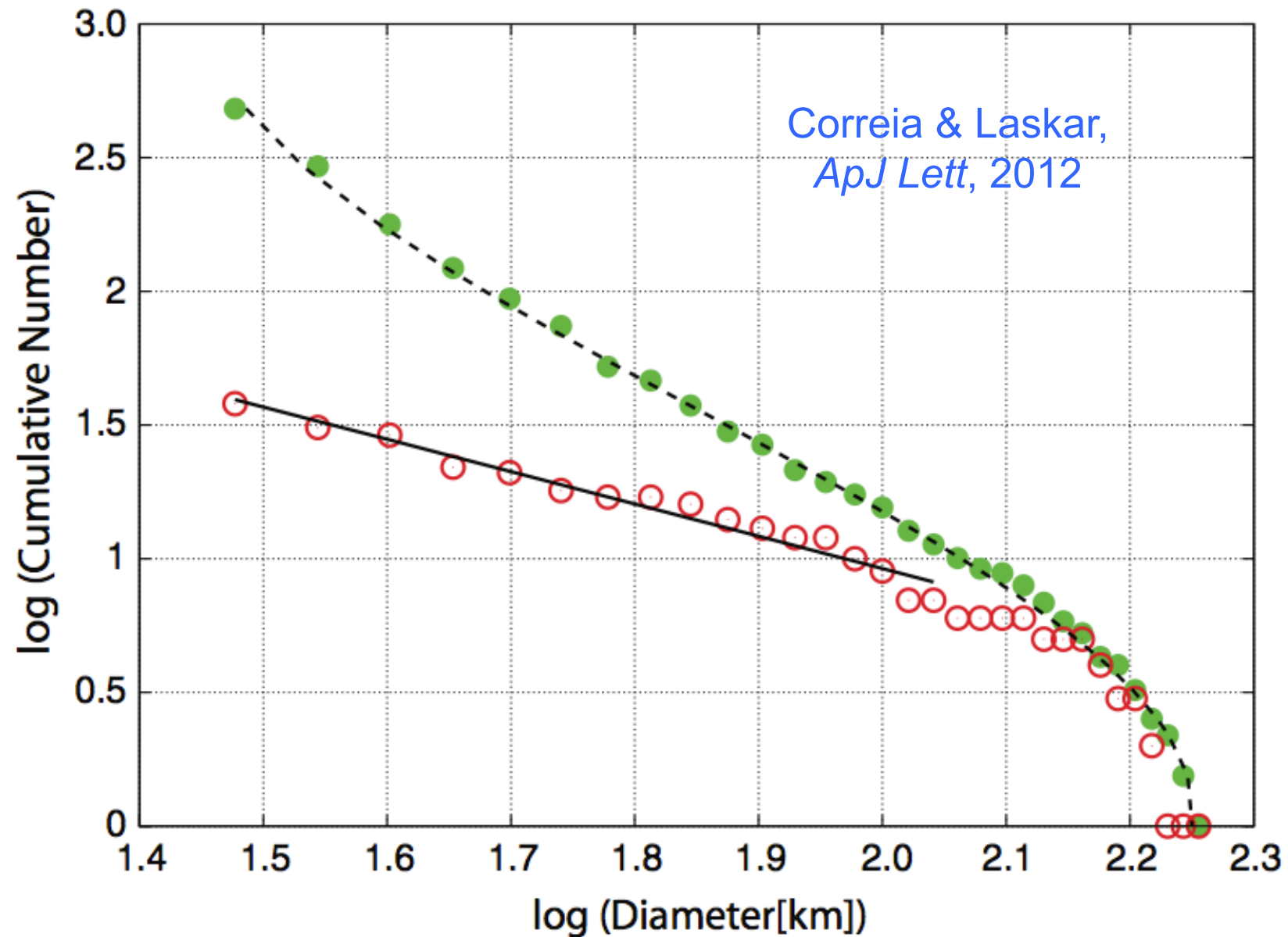


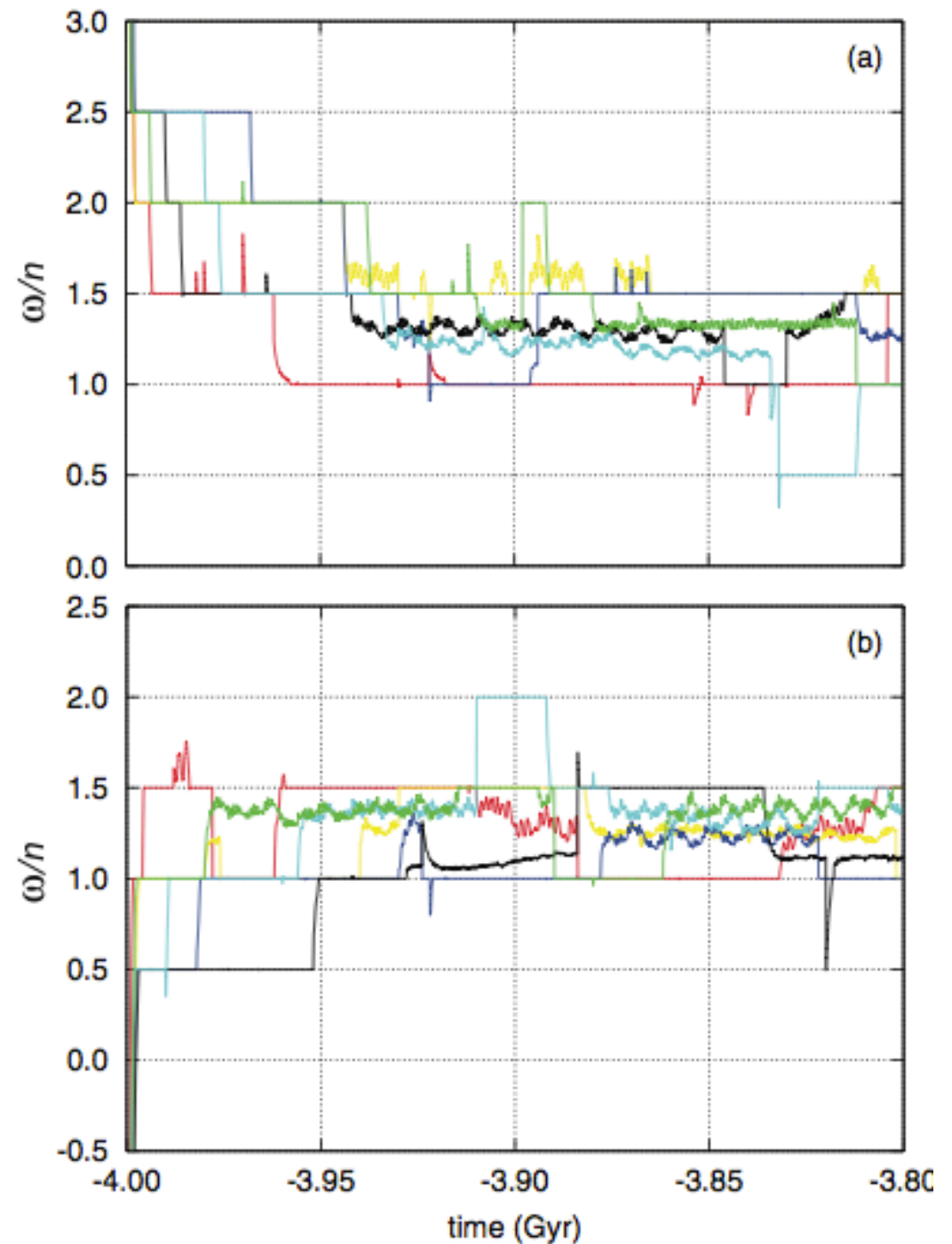
Figure 1. Cumulative number of impacts observed on Mercury's surface (IMD, red), and normalized size distribution in the asteroid-belt (ABD, green). The diameter of the bodies is binned in classes of 5 km.

Correia & Laskar,
ApJ Lett, 2012

Pcap ~ 60 %

Table 2
Critical Eccentricity and Minimal Impactor Diameter
to Destabilize Each Spin–Orbit Resonance

p	$e_{\text{crit.}}$	D (km)	
		$e = 0.1$	$e = 0.2$
5/1	0.211334	—	—
9/2	0.174269	—	14.9
4/1	0.135506	—	17.9
7/2	0.095959	12.2	21.4
3/1	0.057675	16.3	25.5
5/2	0.024877	21.5	30.0
2/1	0.004602	27.9	34.8
3/2	0.000026	35.4	39.3
1/1	—	40.6	41.6
1/2	0.000180	25.7	28.8



VENUS

It is very similar to the Earth:

$$R \approx 0.95 R_T; m \approx 0.82 m_T; g \approx 0.90 g_T$$

but it is closer to the Sun:

$$a \approx 0.72 a_T; P_{\text{orb}} \approx 224.7 \text{ d}$$

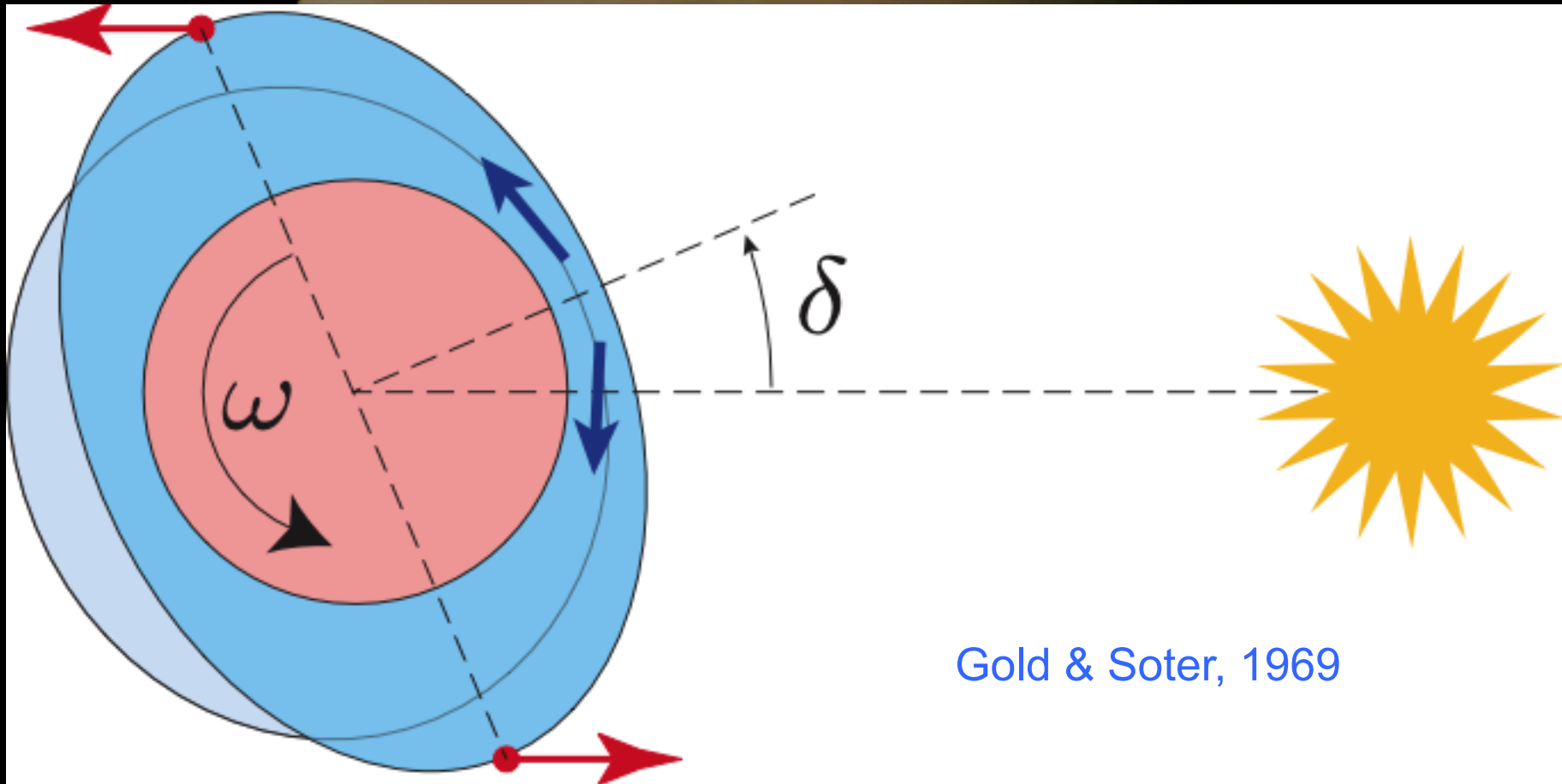
and its atmosphere is quite different:

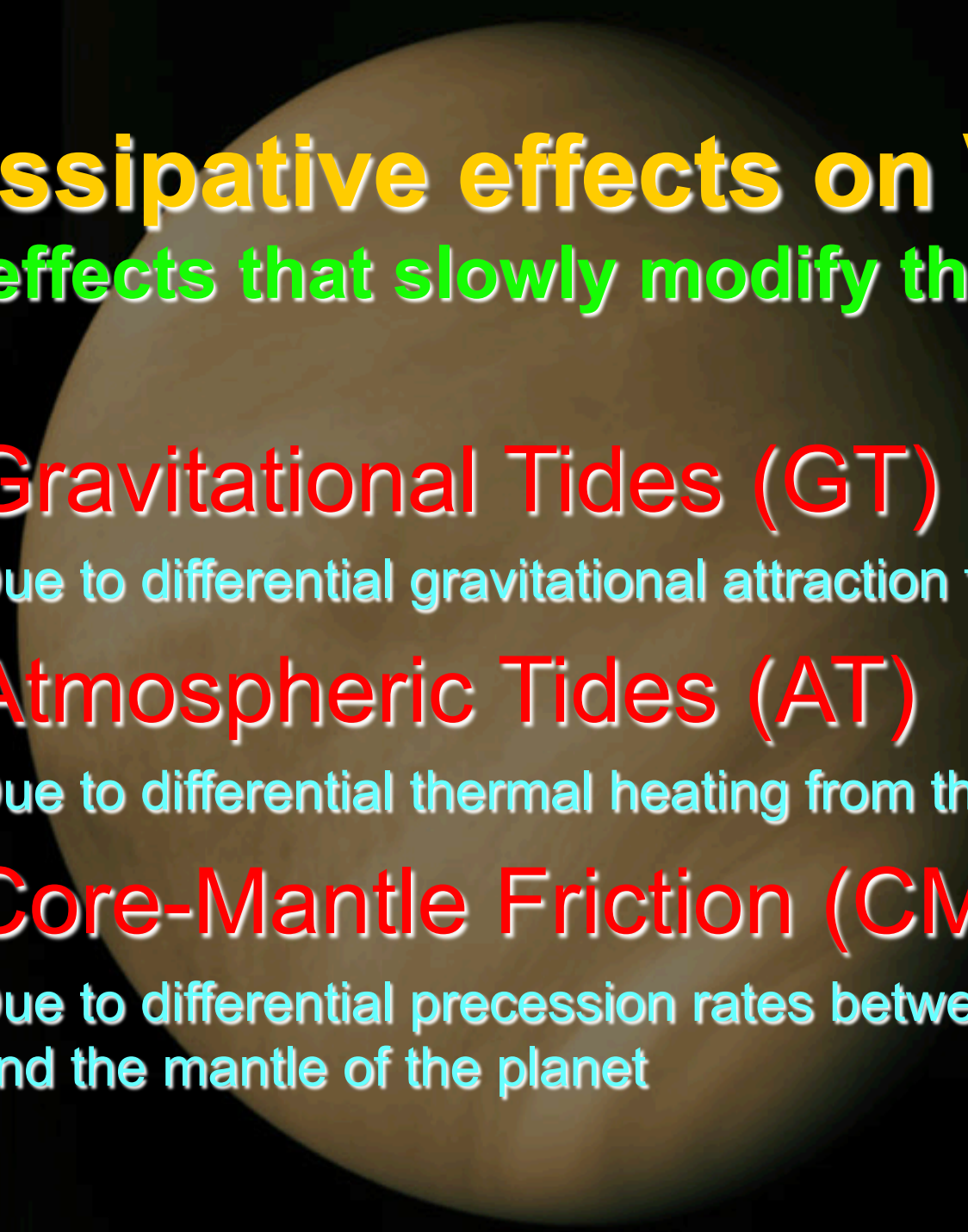
$$A \approx 76\%; \text{CO}_2 \approx 96\%$$

$$T_s \approx 460^\circ\text{C}; p_s \approx 90 \text{ atm}$$

$$P_{\text{rot}} = -243 \text{ day}; \quad \varepsilon = 2,7^\circ$$

thermal atmospheric tides





Dissipative effects on Venus

effects that slowly modify the spin

Gravitational Tides (GT)

Due to differential gravitational attraction from the Sun

Atmospheric Tides (AT)

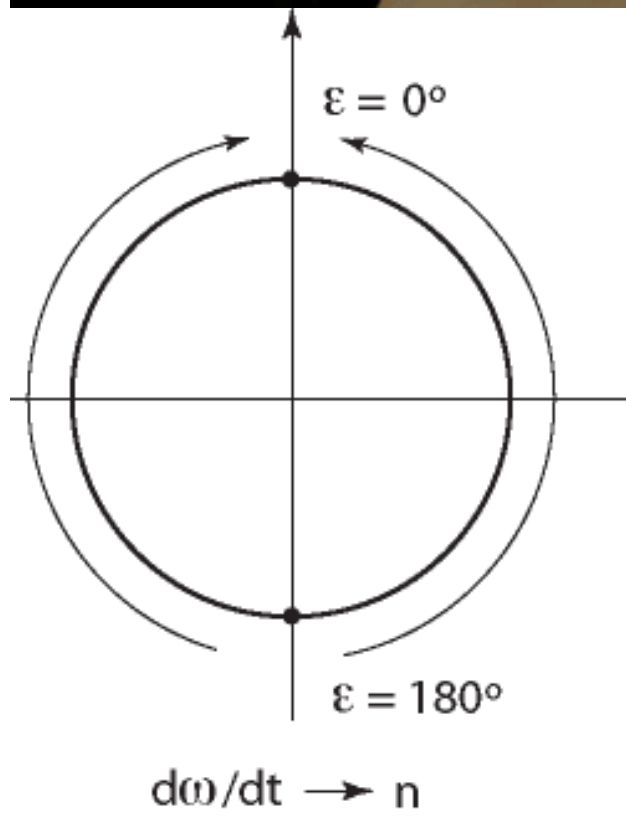
Due to differential thermal heating from the Sun

Core-Mantle Friction (CMF)

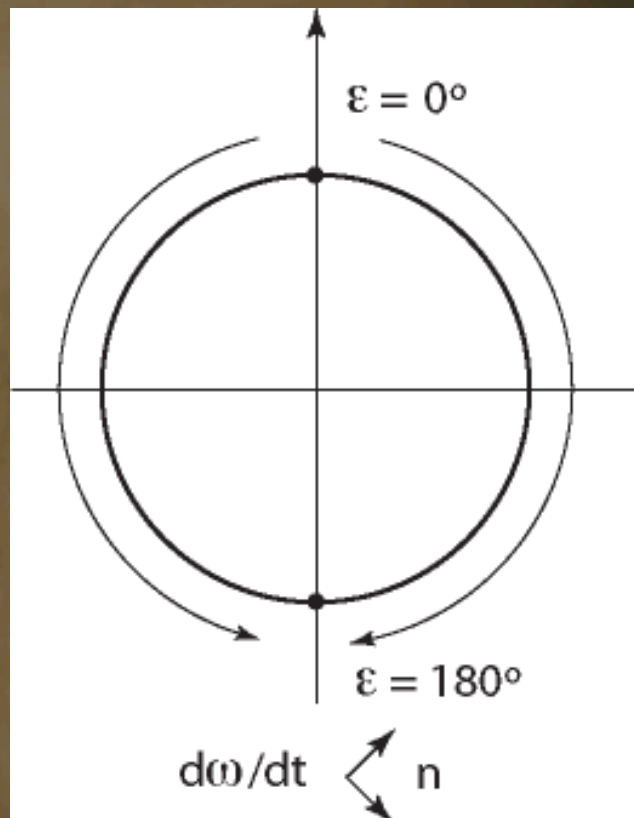
Due to differential precession rates between the core and the mantle of the planet

Main consequences:

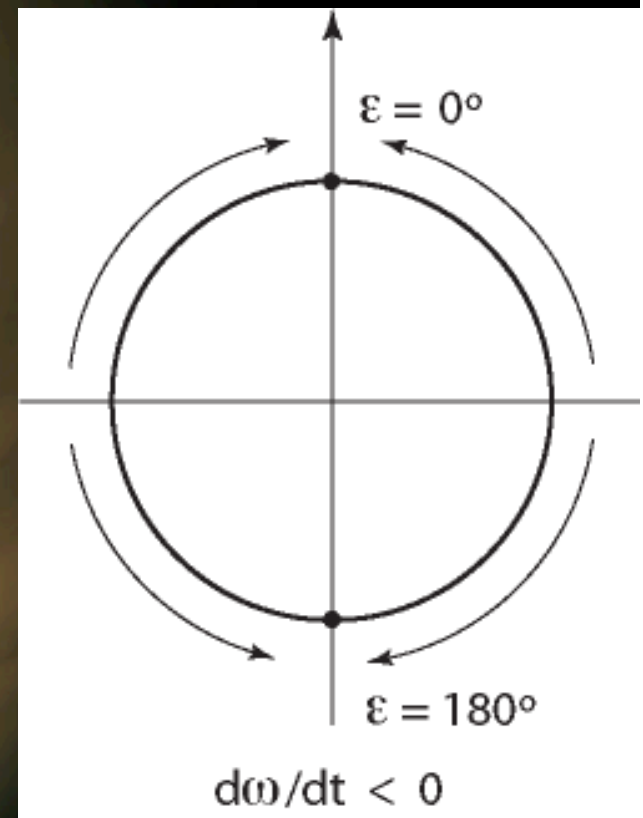
The obliquity will always end at 0° or 180°



GT

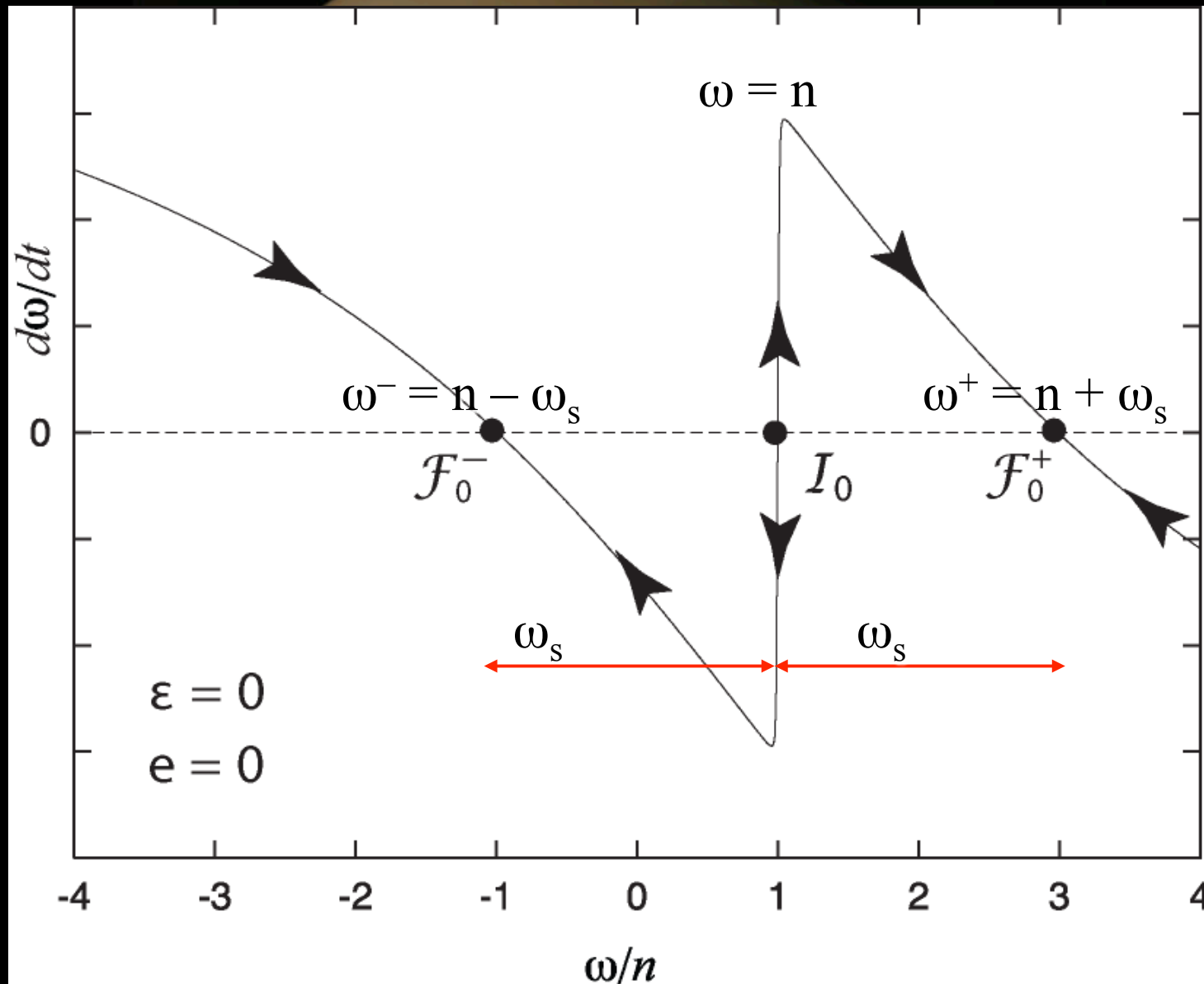


AT



CMF

Equilibrium rotation at 0°

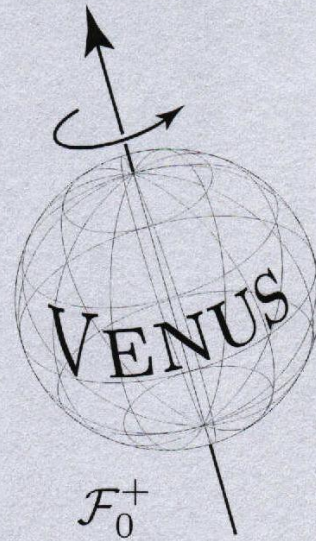


The 4 final spin states of Venus

$P_{\text{rot}} = 76,8 \text{ d}$

$\epsilon = 0^\circ$

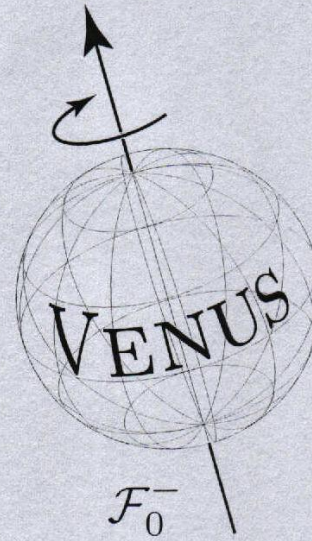
Direct



$P_{\text{rot}} = -243 \text{ d}$

$\epsilon = 0^\circ$

Retrograde



$P_{\text{rot}} = -76,8 \text{ d}$

$\epsilon = 180^\circ$



$P_{\text{rot}} = 243 \text{ d}$

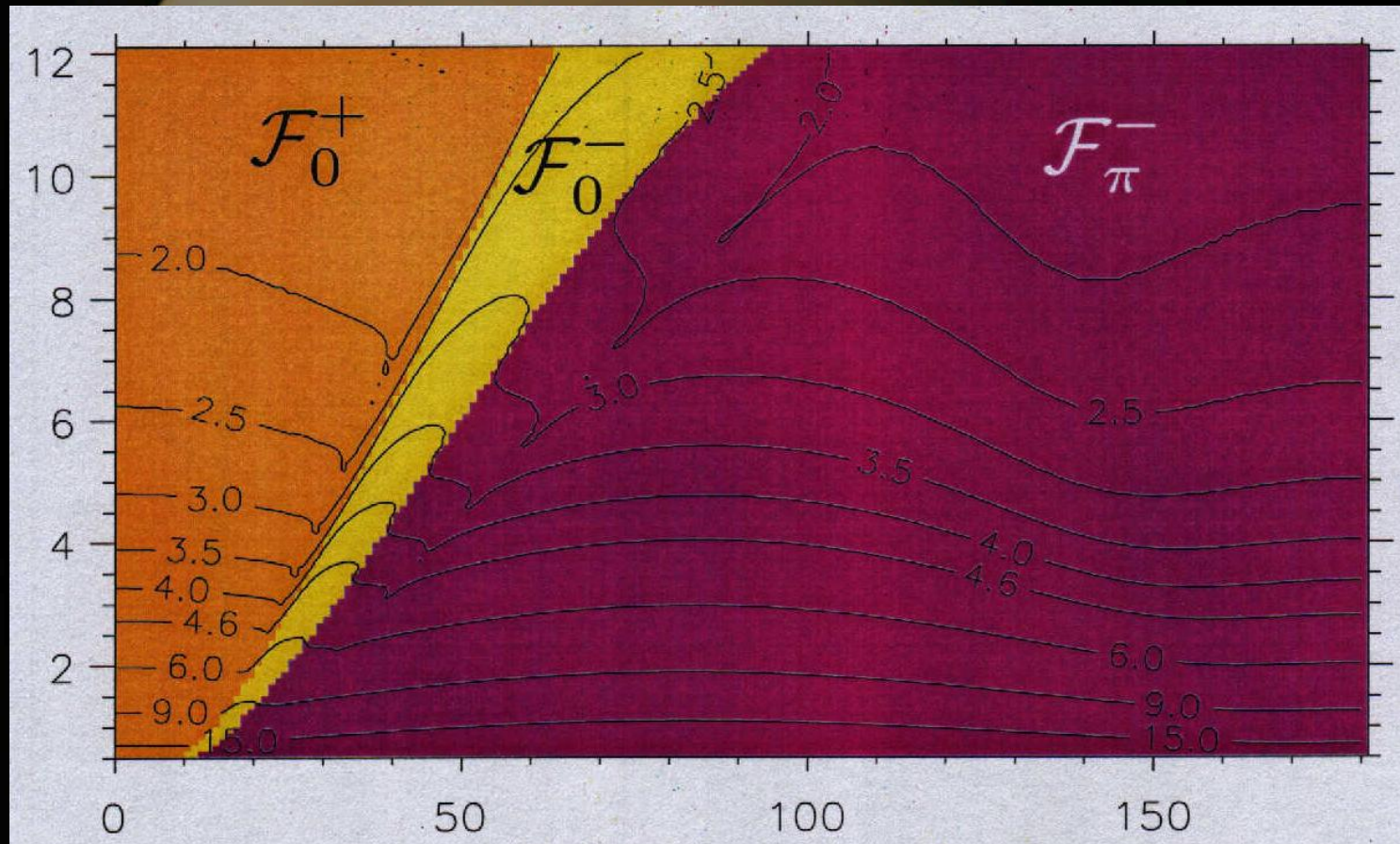
$\epsilon = 180^\circ$



Correia & Laskar,
Nature, 2001

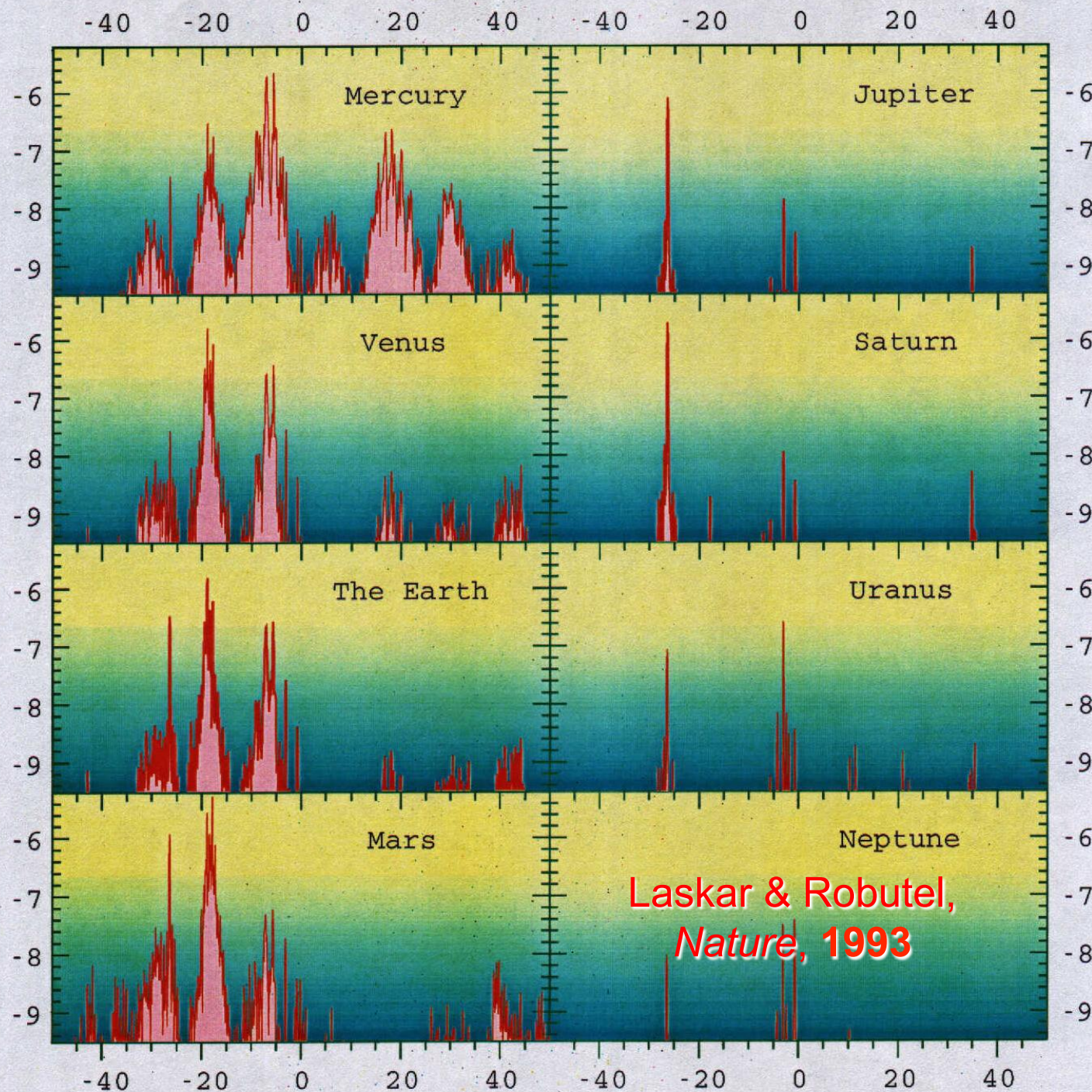
final evolution

Initial period (day)



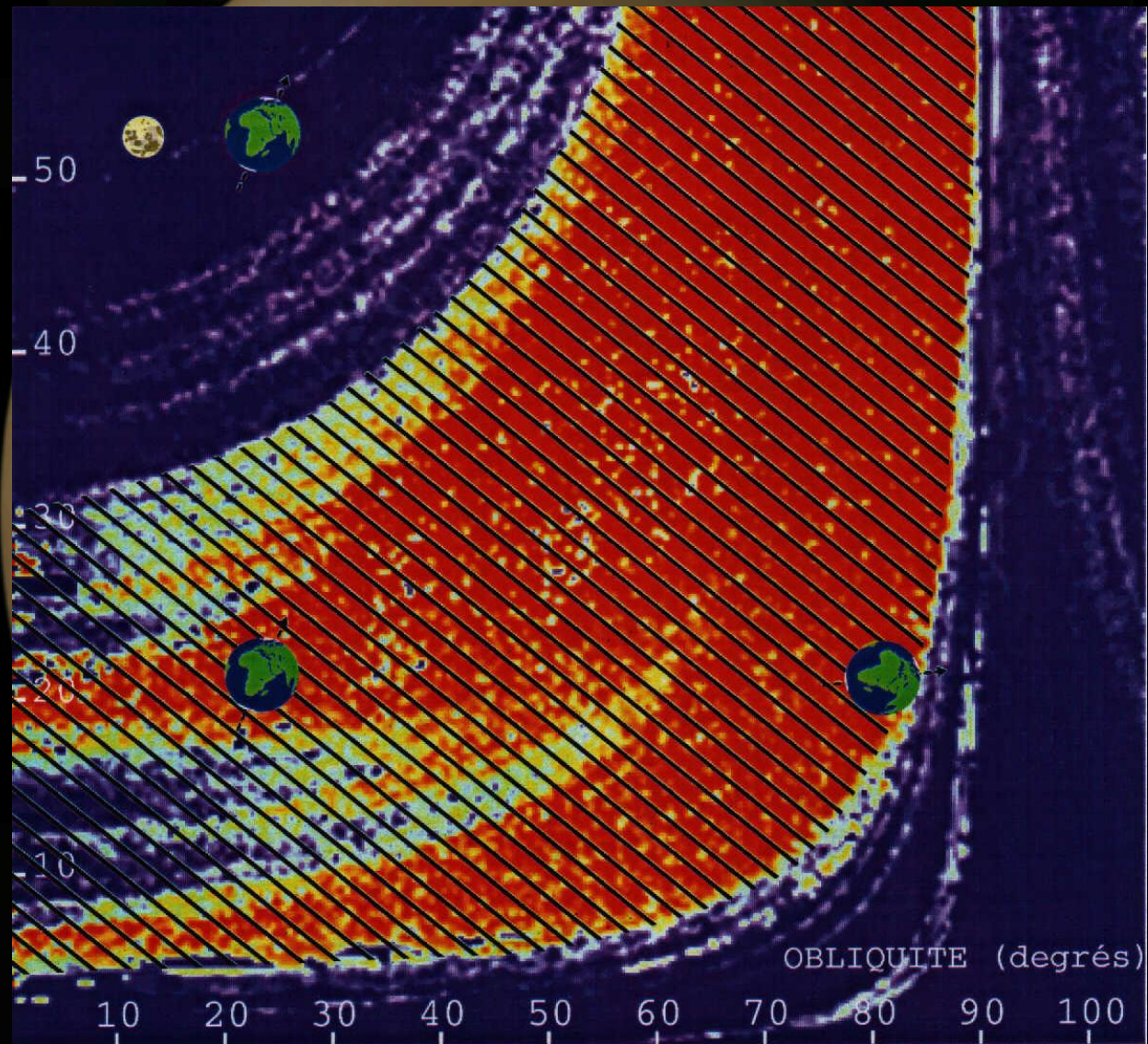
Initial obliquity (degree)

Correia & Laskar,
Nature, 2001



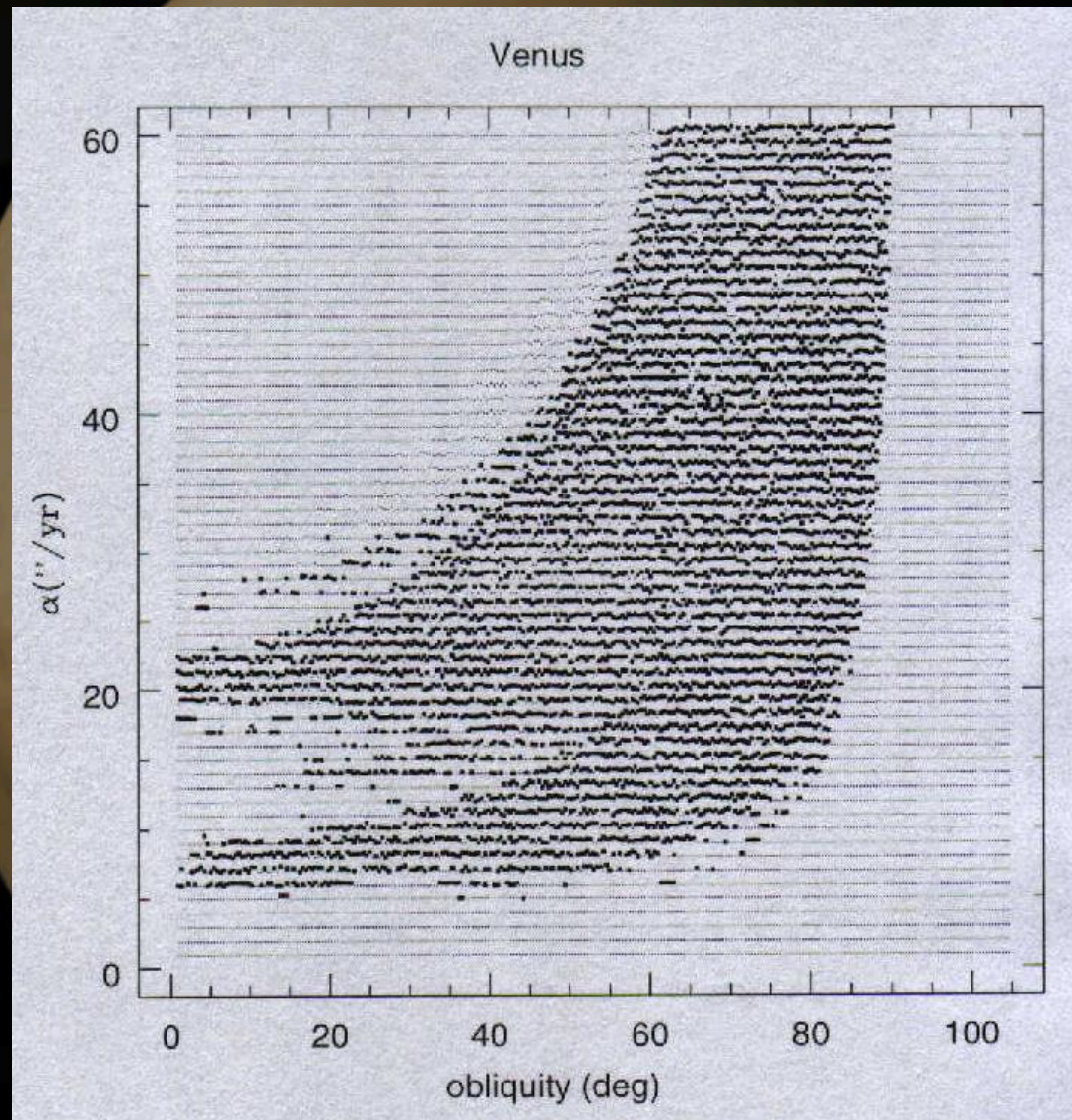
Laskar & Robutel,
Nature, 1993

Earth

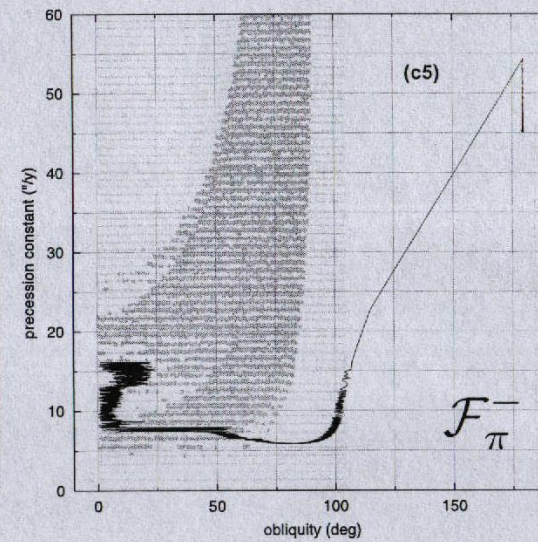
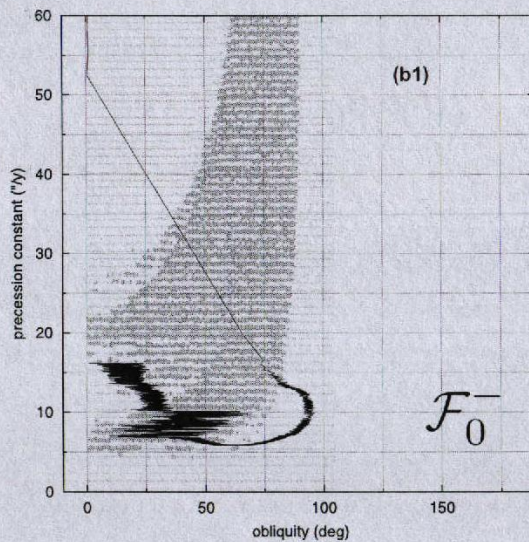
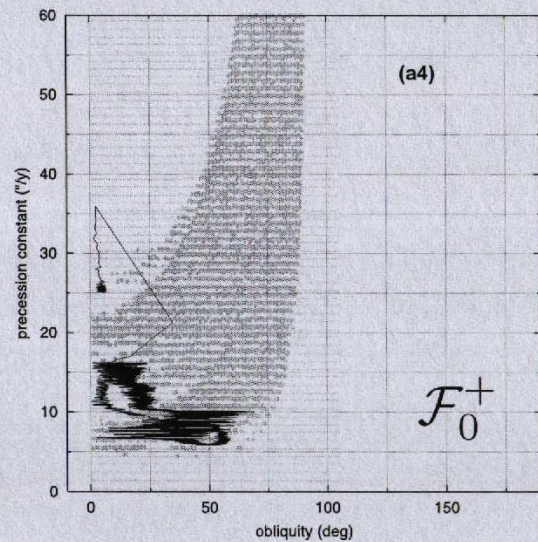
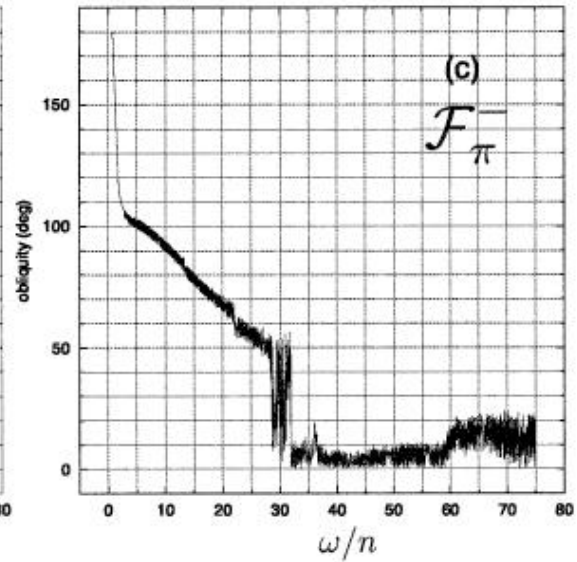
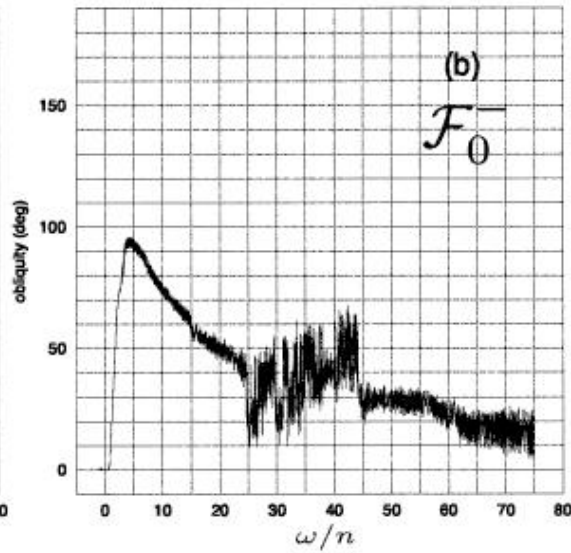
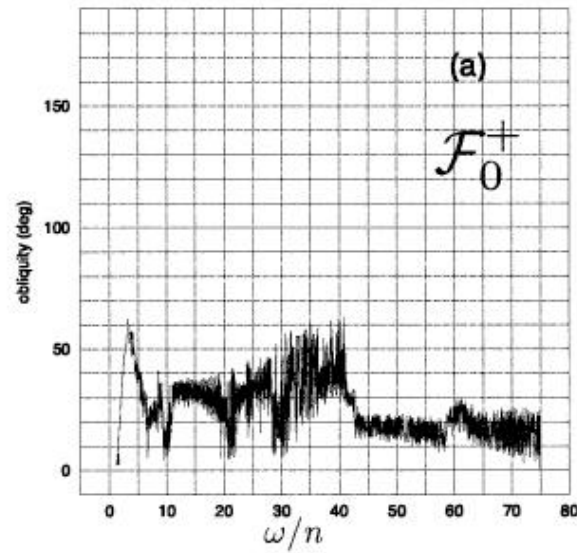


Laskar, Joutel & Robutel, *Nature*, (1993)

Venus



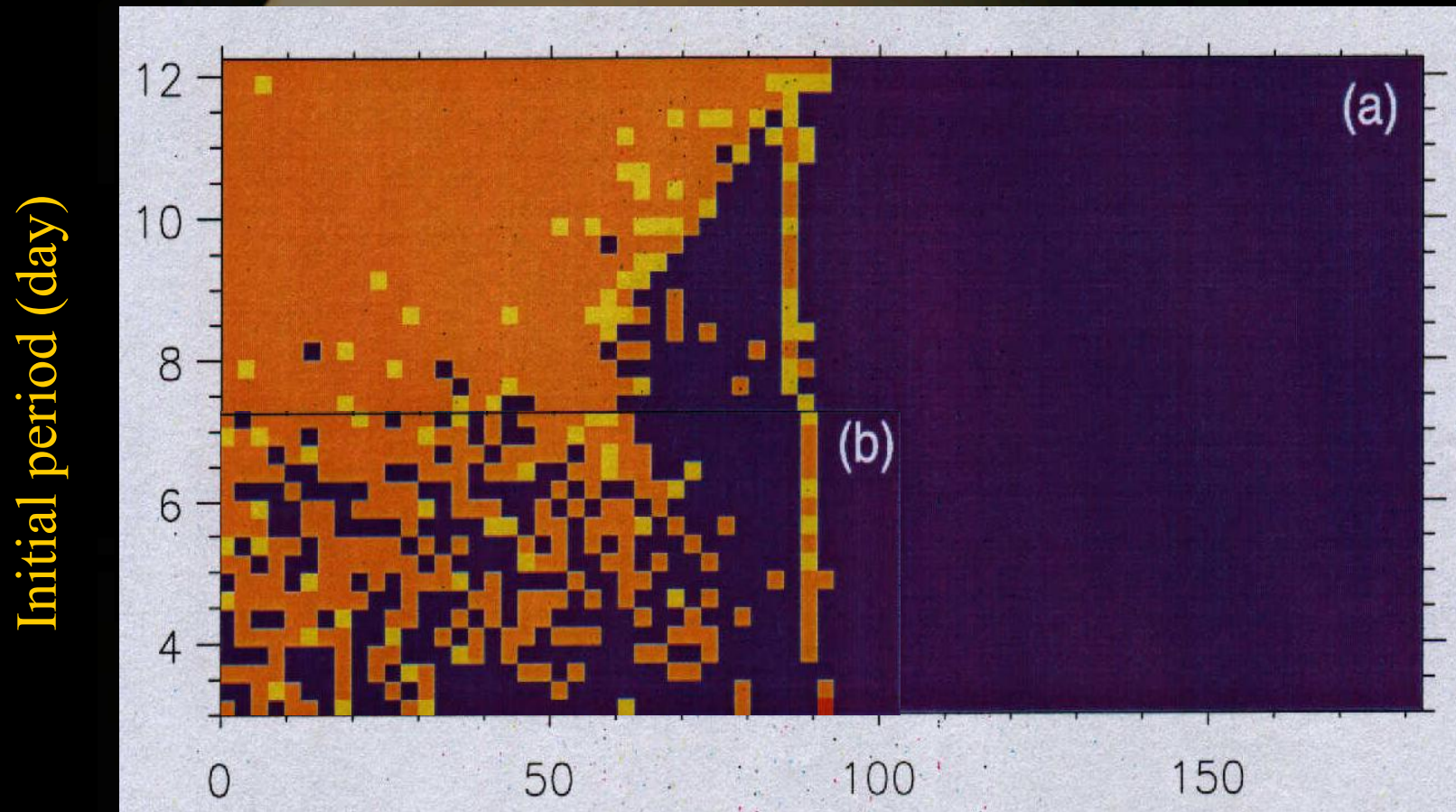
Laskar & Robutel, *Nature*, (1993)



$$\alpha_0 = 16.2''/\text{an} \quad (\mathcal{P}_0 = 3 \text{ jours}) \quad ; \quad \varepsilon_0 = 1^\circ$$

Correia & Laskar, *Icarus*, 2003

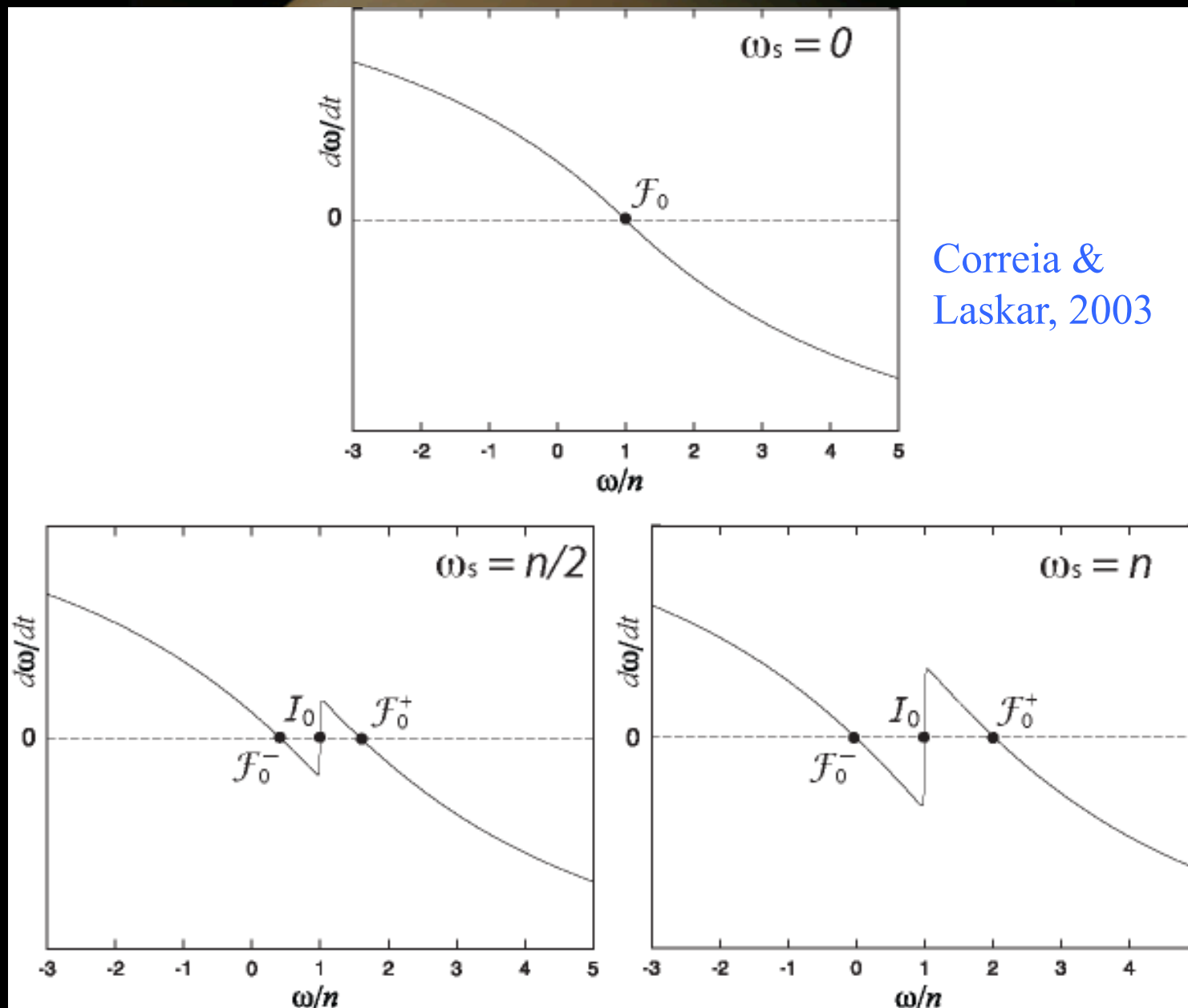
final evolution

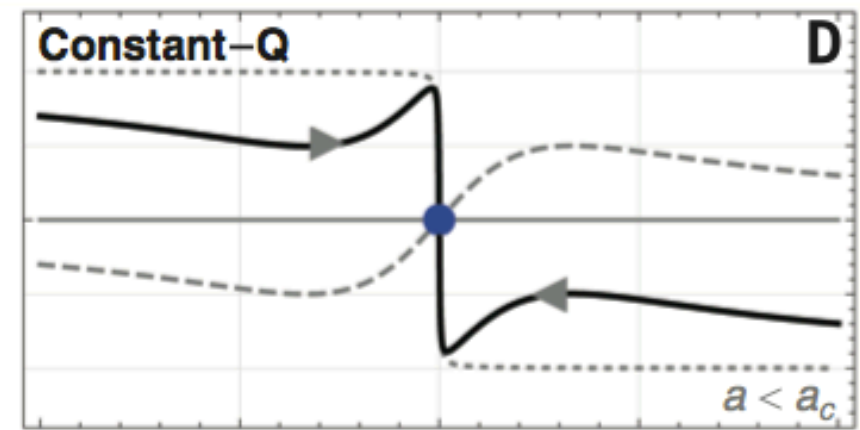
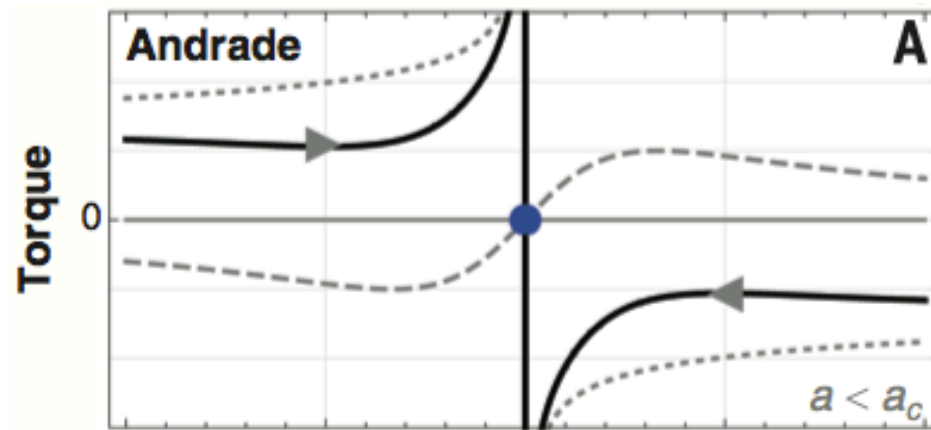


Initial obliquity (degree)

Correia & Laskar,
Nature, 2001

Different tidal strengths

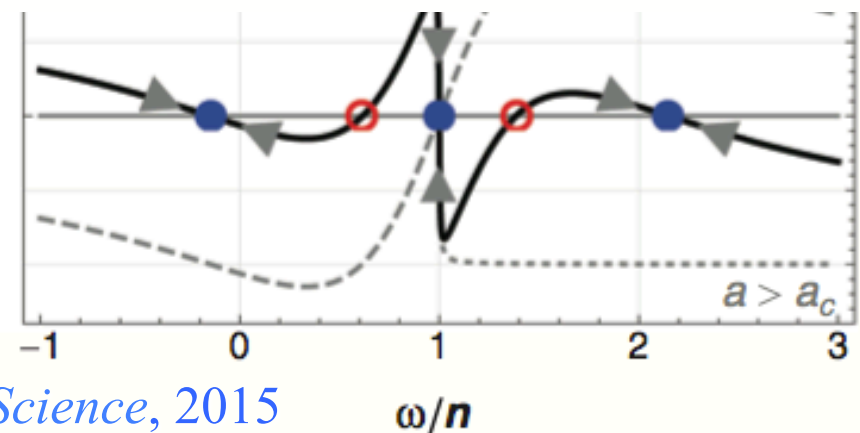
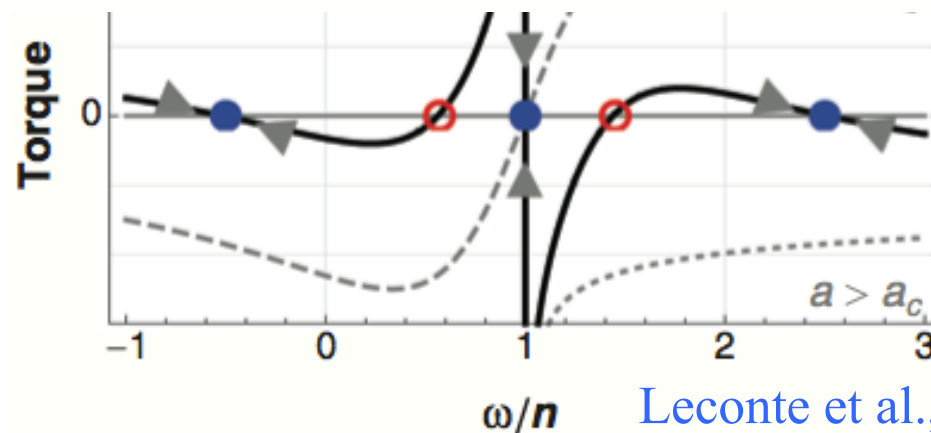




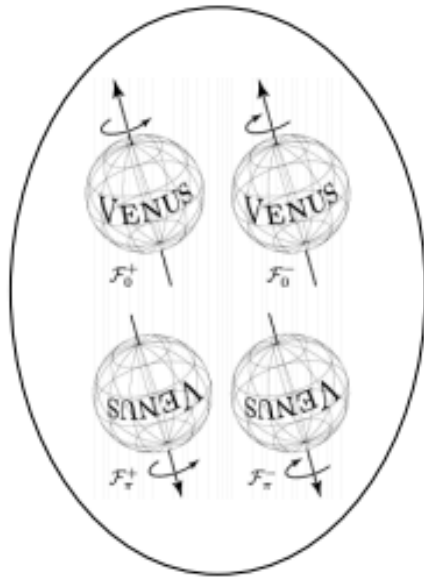
Model output

Sets of simulations

	$F(\text{W.m}^{-2})$	p_s (bar)	q_0 (Pa)	ω_0 (s^{-1})	$2\pi/\omega_0$ (days)
Venus	2610	92	201	3.77×10^{-7}	193
Inner habitable zone	1366	1	1180	2.30×10^{-6}	32
		10	4050	1.46×10^{-6}	50
Outer habitable zone (N_2)	450	1	890	1.18×10^{-6}	62
		10	2960	7.17×10^{-7}	101
Outer habitable zone (CO_2)	450	10	2590	9.7×10^{-7}	70



Leconte et al., *Science*, 2015



**“super-Earths”
should be called
“super-Venus”**

```
/* retourne dans ro (a'/r') *(r/a) */
macro calc_ro {
  efftrunc;
  RsA(n+1); // seul de a'
  rSa = subst( RsA, X, L*Pi**1 )$
  rSa = subst( rSa, Y, L*Pi**1 )$
  rSa = subst( rSa, Z, L*Pi**1 )$
  /* changement de troncature */
  /* changement de variables */
  aSr' = %chgell[aSr'];
  rSa = %chgell[rSa];
  ro = rSa*aSr';
  return ro;
};
```

